

1. Two uniform rods AB and BC are rigidly joined at B so that $\angle ABC = 90^\circ$. Rod AB has length 0.5 m and mass 2 kg. Rod BC has length 2 m and mass 3 kg. The centre of mass of the framework of the two rods is at G .

(a) Find the distance of G from BC .

(2)

The distance of G from AB is 0.6 m.
The framework is suspended from A and hangs freely in equilibrium.

(b) Find the angle between AB and the downward vertical at A .

(3)



2. A lorry of mass 1800 kg travels along a straight horizontal road. The lorry's engine is working at a constant rate of 30 kW. When the lorry's speed is 20 m s^{-1} , its acceleration is 0.4 m s^{-2} . The magnitude of the resistance to the motion of the lorry is R newtons.

(a) Find the value of R .

(4)

The lorry now travels up a straight road which is inclined at an angle α to the horizontal, where $\sin \alpha = \frac{1}{12}$. The magnitude of the non-gravitational resistance to motion is R newtons. The lorry travels at a constant speed of 20 m s^{-1} .

(b) Find the new rate of working of the lorry's engine.

(5)



3.

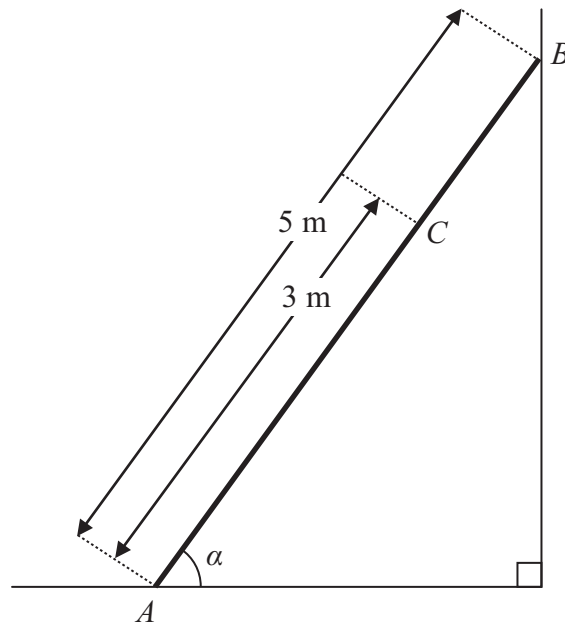


Figure 1

A ladder, of length 5 m and mass 18 kg, has one end A resting on rough horizontal ground and its other end B resting against a smooth vertical wall. The ladder lies in a vertical plane perpendicular to the wall and makes an angle α with the horizontal ground, where $\tan \alpha = \frac{4}{3}$, as shown in Figure 1. The coefficient of friction between the ladder and the ground is μ . A woman of mass 60 kg stands on the ladder at the point C , where $AC = 3$ m. The ladder is on the point of slipping. The ladder is modelled as a uniform rod and the woman as a particle.

Find the value of μ .

(9)



4. At time t seconds the velocity of a particle P is $[(4t-5)\mathbf{i} + 3\mathbf{j}] \text{ m s}^{-1}$. When $t = 0$, the position vector of P is $(2\mathbf{i} + 5\mathbf{j}) \text{ m}$, relative to a fixed origin O .

(a) Find the value of t when the velocity of P is parallel to the vector \mathbf{j} . (1)

(b) Find an expression for the position vector of P at time t seconds. (4)

A second particle Q moves with constant velocity $(-2\mathbf{i} + c\mathbf{j}) \text{ m s}^{-1}$. When $t = 0$, the position vector of Q is $(1\mathbf{i} + 2\mathbf{j}) \text{ m}$. The particles P and Q collide at the point with position vector $(d\mathbf{i} + 14\mathbf{j}) \text{ m}$.

(c) Find (5)

(i) the value of c ,

(ii) the value of d .



Question 4 continued

Lined area for writing the answer to Question 4.

Q4

(Total 10 marks)



5. The point A lies on a rough plane inclined at an angle θ to the horizontal, where $\sin \theta = \frac{24}{25}$. A particle P is projected from A , up a line of greatest slope of the plane, with speed $U \text{ m s}^{-1}$. The mass of P is 2 kg and the coefficient of friction between P and the plane is $\frac{5}{12}$. The particle comes to instantaneous rest at the point B on the plane, where $AB = 1.5 \text{ m}$. It then moves back down the plane to A .

(a) Find the work done against friction as P moves from A to B . (4)

(b) Use the work-energy principle to find the value of U . (4)

(c) Find the speed of P when it returns to A . (3)



Question 5 continued

Lined area for writing the answer to Question 5 continued.

(Total 11 marks)

Q5

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6.

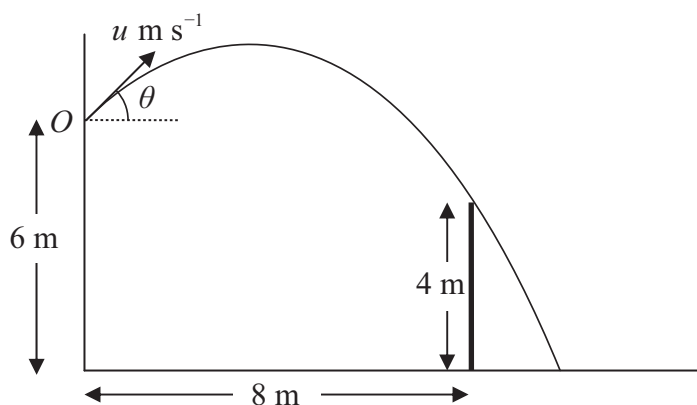


Figure 2

A ball is thrown from a point O , which is 6 m above horizontal ground. The ball is projected with speed $u \text{ m s}^{-1}$ at an angle θ above the horizontal. There is a thin vertical post which is 4 m high and 8 m horizontally away from the vertical through O , as shown in Figure 2. The ball passes just above the top of the post 2 s after projection. The ball is modelled as a particle.

(a) Show that $\tan \theta = 2.2$ **(5)**

(b) Find the value of u . **(2)**

The ball hits the ground T seconds after projection.

(c) Find the value of T . **(3)**

Immediately before the ball hits the ground the direction of motion of the ball makes an angle α with the horizontal.

(d) Find α . **(5)**



7. A particle A of mass m is moving with speed u on a smooth horizontal floor when it collides directly with another particle B , of mass $3m$, which is at rest on the floor. The coefficient of restitution between the particles is e . The direction of motion of A is reversed by the collision.

- (a) Find, in terms of e and u ,
 - (i) the speed of A immediately after the collision,
 - (ii) the speed of B immediately after the collision.

(7)

After being struck by A the particle B collides directly with another particle C , of mass $4m$, which is at rest on the floor. The coefficient of restitution between B and C is $2e$. Given that the direction of motion of B is reversed by this collision,

- (b) find the range of possible values of e ,
- (c) determine whether there will be a second collision between A and B .

(6)

(3)



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Question 7 continued

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(Total 16 marks)

TOTAL FOR PAPER: 75 MARKS

Q7

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