## C1 -Sequences Series PPQ's

2. The sequence of positive numbers $u_{1}, u_{2}, u_{3}, \ldots$, is given by

$$
u_{n+1}=\left(u_{n}-3\right)^{2}, \quad u_{1}=1
$$

(a) Find $u_{2}, u_{3}$ and $u_{4}$.
(b) Write down the value of $u_{20}$.
4. A sequence $a_{1}, a_{2}, a_{3}, \ldots$ is defined by

$$
\begin{aligned}
& a_{1}=3 \\
& a_{n+1}=3 a_{n}-5, \quad n \geq 1
\end{aligned}
$$

(a) Find the value $a_{2}$ and the value of $a_{3}$.
(b) Calculate the value of $\sum_{r=1}^{5} a_{r}$.
4. A girl saves money over a period of 200 weeks. She saves 5 p in Week $1,7 \mathrm{p}$ in Week 2, $9 p$ in Week 3, and so on until Week 200. Her weekly savings form an arithmetic sequence.
(a) Find the amount she saves in Week 200
(b) Calculate her total savings over the complete 200 week period.
7. An athlete prepares for a race by completing a practice run on each of 11 consecutive days. On each day after the first day he runs further than he ran on the previous day. The lengths of his 11 practice runs form an arithmetic sequence with first term $a \mathrm{~km}$ and common difference $d \mathrm{~km}$.

He runs 9 km on the 11th day, and he runs a total of 77 km over the 11 day period.
Find the value of $a$ and the value of $d$.
7. On Alice's 11 th birthday she started to receive an annual allowance. The first annual allowance was $£ 500$ and on each following birthday the allowance was increased by $£ 200$.
(a) Show that, immediately after her 12th birthday, the total of the allowances that Alice had received was $£ 1200$.
(b) Find the amount of Alice's annual allowance on her 18th birthday.
(c) Find the total of the allowances that Alice had received up to and including her 18th birthday.

When the total of the allowances that Alice had received reached $£ 32000$ the allowance stopped.
(d) Find how old Alice was when she received her last allowance.
8. A sequence $a_{1}, a_{2}, a_{3}, \ldots$ is defined by

$$
\begin{aligned}
a_{1} & =k \\
a_{n+1} & =3 a_{n}+5, \quad n \geqslant 1
\end{aligned}
$$

where $k$ is a positive integer
(a) Write down an expression for $a_{2}$ in terms of $k$.
-
(b) Show that $a_{3}=9 k+20$.
(c) (i) Find $\sum_{r=1}^{4} a_{r}$ in terms of $k$.
(ii) Show that $\sum_{r=1}^{4} a_{r}$ is divisible by 10 .
9. An arithmetic series has first term $a$ and common difference $d$.
(a) Prove that the sum of the first $n$ terms of the series is

$$
\frac{1}{2} n[2 a+(n-1) d]
$$

Sean repays a loan over a period of $n$ months. His monthly repayments form an arithmetic sequence.
He repays $£ 149$ in the first month, $£ 147$ in the second month, $£ 145$ in the third month, and so on. He makes his final repayment in the $n$th month, where $n>21$.
(b) Find the amount Sean repays in the 21 st month.

Over the $n$ months, he repays a total of $£ 5000$.
(c) Form an equation in $n$, and show that your equation may be written as

$$
\begin{equation*}
n^{2}-150 n+5000=0 \tag{3}
\end{equation*}
$$

(d) Solve the equation in part (c).
(3)
(e) State, with a reason, which of the solutions to the equation in part (c) is not a sensible solution to the repayment problem.
(1)

9．Ann has some sticks that are all of the same length．She arranges them in squares and has made the following 3 rows of patterns：

Row 1
Row 2
Row 3
She notices that 4 sticks are required to make the single square in the first row， 7 sticks to make 2 squares in the second row and in the third row she needs 10 sticks to make 3 squares．
（a）Find an expression，in terms of $n$ ，for the number of sticks required to make a similar arrangement of $n$ squares in the $n$th row．

Ann continues to make squares following the same pattern．She makes 4 squares in the th row and so on until she has completed 10 rows．
（b）Find the total number of sticks Ann uses in making these 10 rows．

Ann started with 1750 sticks．Given that Ann continues the pattern to complete $k$ rows but does not have sufficient sticks to complete the $(k+1)$ th row，
（c）show that $k$ satisfies $(3 k-100)(k+35)<0$ ．
（d）Find the value of $k$ ．

11．The first term of an arithmetic sequence is 30 and the common difference is -1.5
（a）Find the value of the 25 th term．

The $r$ th term of the sequence is 0 ．
（b）Find the value of $r$ ．

The sum of the first $n$ terms of the sequence is $S_{n}$
（c）Find the largest positive value of $S_{n}$ ．

ToP） 0096 （D）00b1（ 9 ）ont（D）（C）
$s / 20+1 \cdot 0=P$＇$s=0$（ $t$ ）
oo．Son assent（ 9 ）deon（b）（c）
\＆t（a）ヒ＇ウ（D）（2）
H（9）カ＇1ヶク（0）（1）


