- SEQUENCES & SERIES PPQ'S

2. The sequence of positive numbers $u_1, u_2, u_3, ...,$ is given by

$$u_{n+1} = (u_n - 3)^2, \qquad u_1 = 1$$

(a) Find u_2 , u_3 and u_4 .

(b) Write down the value of u_{20} .

4. A sequence a_1, a_2, a_3, \ldots is defined by

 $a_{n+1} = 3a_n - 5, \quad n \ge 1.$

 $a_1 = 3$.

- (a) Find the value a_2 and the value of a_3 .
- (b) Calculate the value of $\sum_{r=1}^{5} a_r$.

4. A girl saves money over a period of 200 weeks. She saves 5p in Week 1, 7p in Week 2, 9p in Week 3, and so on until Week 200. Her weekly savings form an arithmetic sequence.
(a) Find the amount she saves in Week 200. (3)

(b) Calculate her total savings over the complete 200 week period.

7. An athlete prepares for a race by completing a practice run on each of 11 consecutive days. On each day after the first day he runs further than he ran on the previous day. The lengths of his 11 practice runs form an arithmetic sequence with first term a km and common difference d km.

He runs 9 km on the 11th day, and he runs a total of 77 km over the 11 day period.

Find the value of a and the value of d.

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(7)

(3)

(1)

(2)

(3)

Leave blank

(3)

- On Alice's 11th birthday she started to receive an annual allowance. The first annual allowance 7. was £500 and on each following birthday the allowance was increased by £200.
 - (a) Show that, immediately after her 12th birthday, the total of the allowances that Alice had received was £1200. (1)
 - (b) Find the amount of Alice's annual allowance on her 18th birthday.
 - (c) Find the total of the allowances that Alice had received up to and including her 18th birthday.

When the total of the allowances that Alice had received reached £32 000 the allowance stopped.

- (d) Find how old Alice was when she received her last allowance.
 - 8. A sequence a_1, a_2, a_3, \dots is defined by $a_1 = k$, $a_1 = \kappa,$ $a_{n+1} = 3a_n + 5, \qquad n \ge 1,$ where k is a positive integer. (a) Write down an expression for a_2 in terms of k. (1) (b) Show that $a_3 = 9k + 20$. (2)(c) (i) Find $\sum_{r=1}^{4} a_r$ in terms of k. (ii) Show that $\sum_{r=1}^{4} a_r$ is divisible by 10. (4)

9. An arithmetic series has first term a and common difference d. (a) Prove that the sum of the first *n* terms of the series is $\frac{1}{2}n[2a+(n-1)d].$ Sean repays a loan over a period of n months. His monthly repayments form an arithmetic sequence. He repays £149 in the first month, £147 in the second month, £145 in the third month, and so on. He makes his final repayment in the *n*th month, where n > 21. (b) Find the amount Sean repays in the 21st month.

Over the n months, he repays a total of £5000.

(c) Form an equation in n, and show that your equation may be written as

 $n^2 - 150n + 5000 = 0.$

(d) Solve the equation in part (c).

(e) State, with a reason, which of the solutions to the equation in part (c) is not a sensible solution to the repayment problem. (1) (7)

(4)

(2)

(3)

(3)

(2)

(3)

Row 1	Π		,				
KOW 1							
Row 2							
Row 3							
She notices that 4 sticks are required to make the single square in the first row, 7 sticks to make 2 squares in the second row and in the third row she needs 10 sticks to make 3 squares.							
(a) Find a	in expression,	in terms of n , t	for the numbe	r of sticks	required	to make	a simila
arrang	gement of <i>n</i> so	uares in the <i>n</i> t	h row.				(3
Ann continues to make squares following the same pattern. She makes 4 squares in the 4th row and so on until she has completed 10 rows.							
(b) Find the total number of sticks Ann uses in making these 10 rows.							
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Ann starte but does n (c) show (d) Find t	ed with 1750 s ot have suffic that k satisfies the value of k. 1. The first term of (a) Find the va The rth term of (b) Find the va	sticks. Given the sequence is 0.	that Ann cont omplete the (<i>i</i> - 35) < 0.	inues the p k+1)th rov	attern to	o complet	e <i>k</i> row (4

(d)(a) -6, (b) 21 (c) 315. SE (P) St1 (9) 1-46 (D) 3 6017(9) (t) (C) (C) 3K+2 (P) 2K+50 (C) 100K+20